

Those online enjoy an **advantage**.

Digital inclusion provides new opportunities,
in education, employment, health, and social well-being.

The distribution of broadband may **strengthen** or **reduce** inequality

How can we quantify the **effects** of broadband access **on inequality**?

Inequality is a transitive irreflexive relation $b < a$.

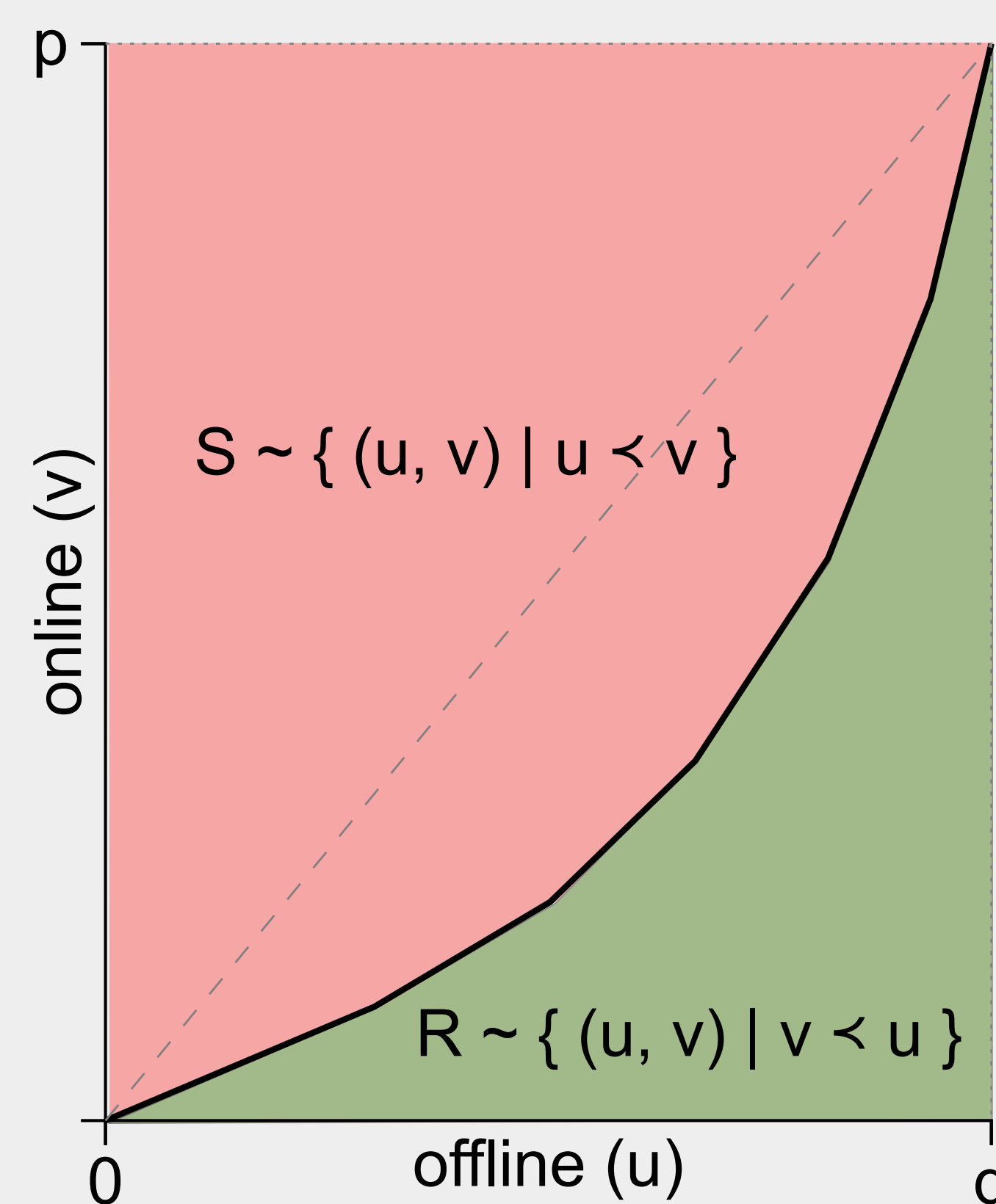
Consider two households,
with b more deprived than a : $b < a$

If b is online, while a is offline, then b 's
digital advantage **R**educes existing
inequality.

If a is online, while b is offline, then b 's
digital disadvantage **S**trengthens
existing inequality.

A *shuffle graph* plots cumulative
households online against cumulative
households offline, for each level of
deprivation, to give a *Lorenz curve*.

The area **S** above the curve represents the offline-online pairs that
Strengthen inequality, while the area **R** below represents the **R**eductions



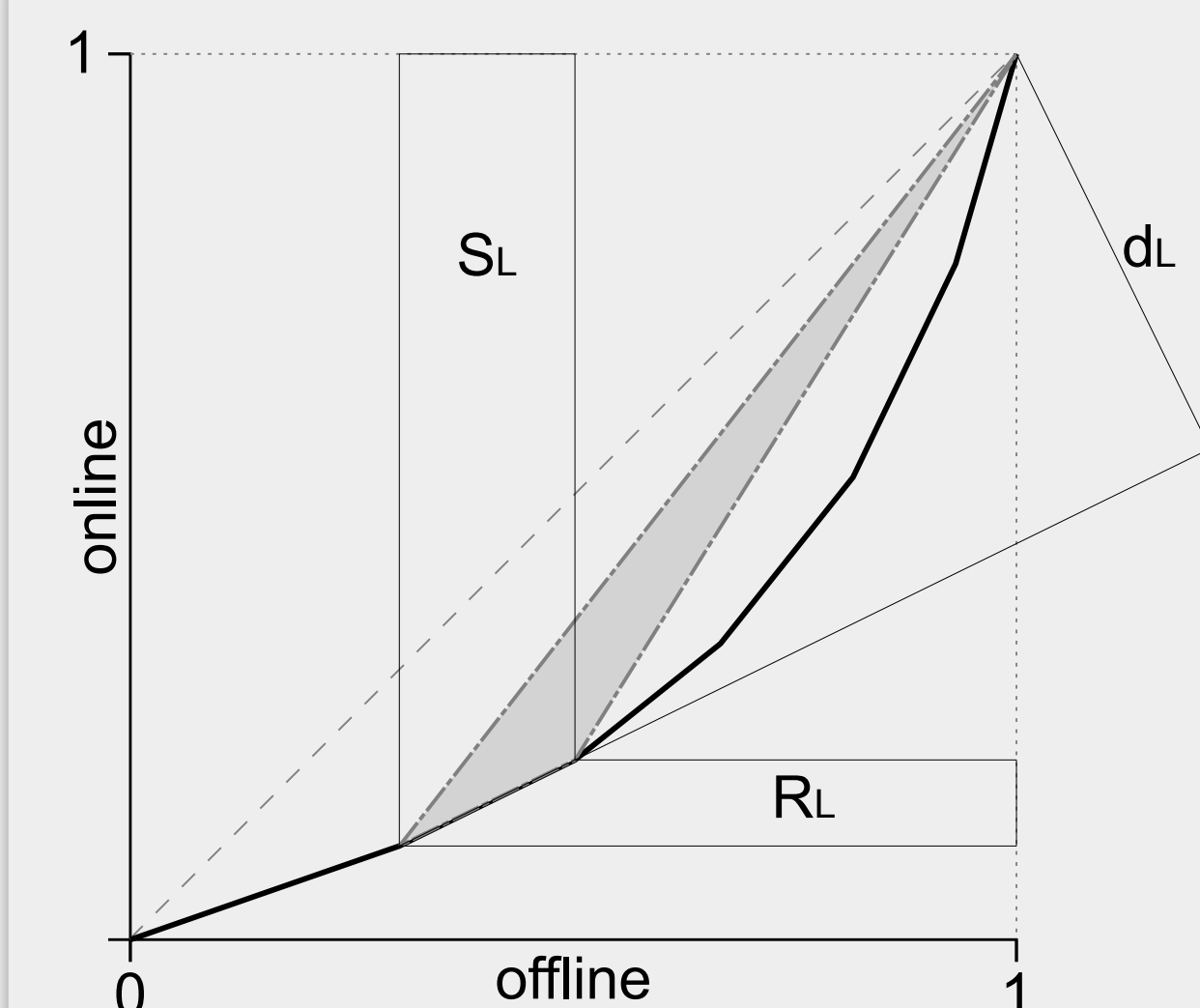
The normalised difference $(S-R) / (S+R)$ is the **depth of the divide**.

We interpret the depth of the divide as a measure of the deprivation-related
barriers to inclusion. It is normalised to take values in the range $[-1, 1]$,

Depth is a **relative measure**:
it quantifies the deprivation of the offline population, relative to those online.

An **absolute measure** of the net contribution of the digital divide to inequality
is given by comparing $(S - R)$ to the value $P^2 / 4$ for the extreme case in
which the most deprived half of the population is offline, and the rest are
online, so that every offline household is more deprived than every online
household. We define the **breadth of the divide**, to give range $[-1, 1]$:

$$4 \times (S-R) / P^2$$



The depth of the divide.

Here, the shuffle graph is scaled to the unit
square. $(S - R)$ is twice the area enclosed by the
Lorenz curve and the line of perfect equality.

The net effect of the divide on a local population,
 L , is proportional to the area of the shaded
triangle in the diagram, which is equal to

$$(S_L - R_L) / 2.$$

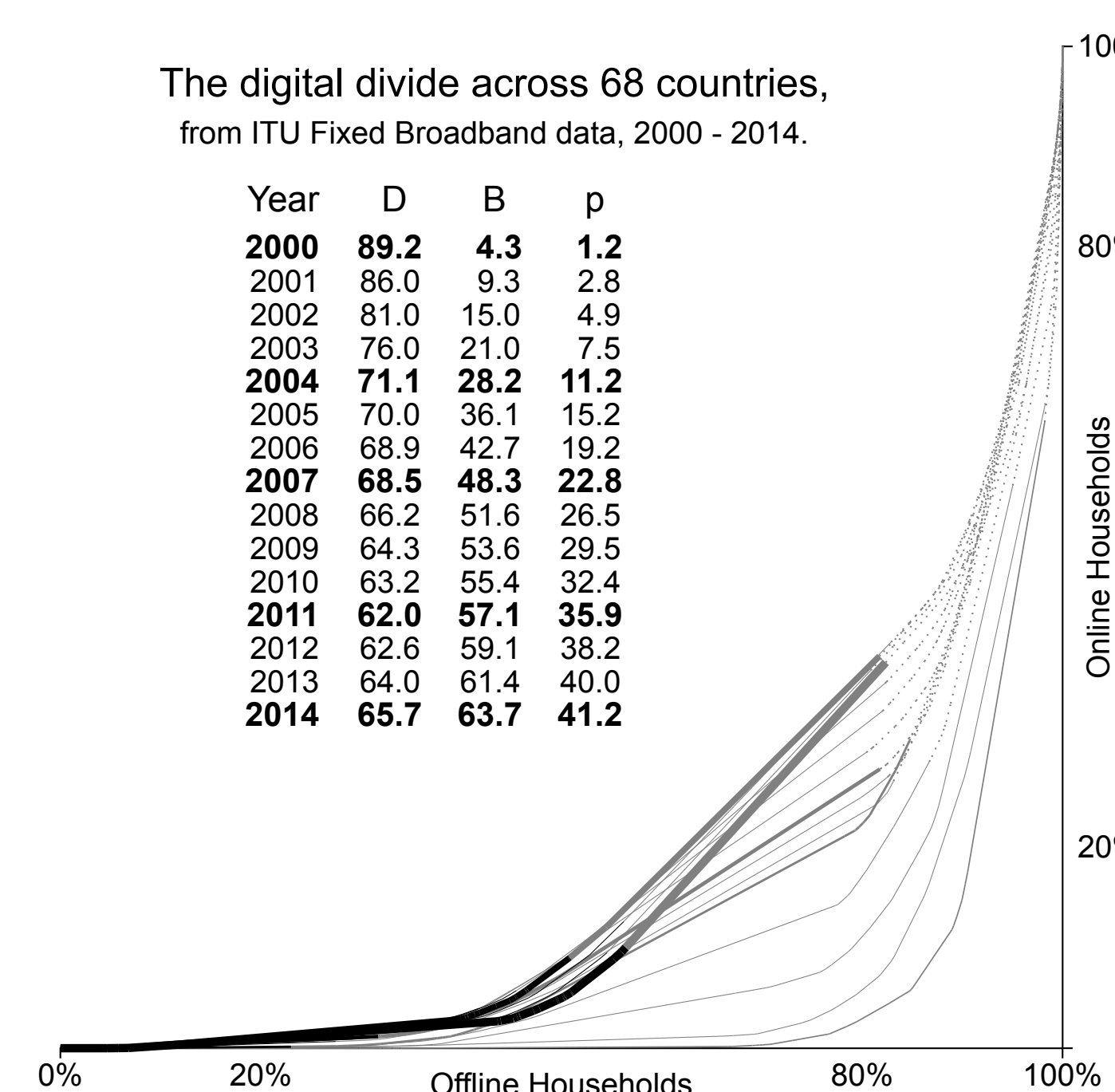
The height of the triangle, d_L , gives a local
measure of depth.

Y	1990	1994	1998	1999	2001	2002
p	15.9%	22.6%	36.6%	42.1%	51.0%	56.5%
C	40%	39%	31%	30%	26%	23%
B	25.4%	35.3%	45.4%	50.5%	53.0%	52.0%
D	47.6%	50.4%	48.9%	51.8%	53.1%	52.9%

USA Home computer uptake

The digital divide across 68 countries,
from ITU Fixed Broadband data, 2000 - 2014.

Year	D	B	p
2000	89.2	4.3	1.2
2001	86.0	9.3	2.8
2002	81.0	15.0	4.9
2003	76.0	21.0	7.5
2004	71.1	28.2	11.2
2005	70.0	36.1	15.2
2006	68.9	42.7	19.2
2007	68.5	48.3	22.8
2008	66.2	51.6	26.5
2009	64.3	53.6	29.5
2010	63.2	55.4	32.4
2011	62.0	57.1	35.9
2012	62.6	59.1	38.2
2013	64.0	61.4	40.0
2014	65.7	63.7	41.2



Results

An early analysis of computer usage 1990-2002, using the Concentration
Index, presented a rosy picture of falling inequality, globally and locally.
Revisiting the data for home computer usage, we find that the breadth of the
divide, which we interpret as its societal impact, grew significantly. The depth
of this divide also grew, until 2001.

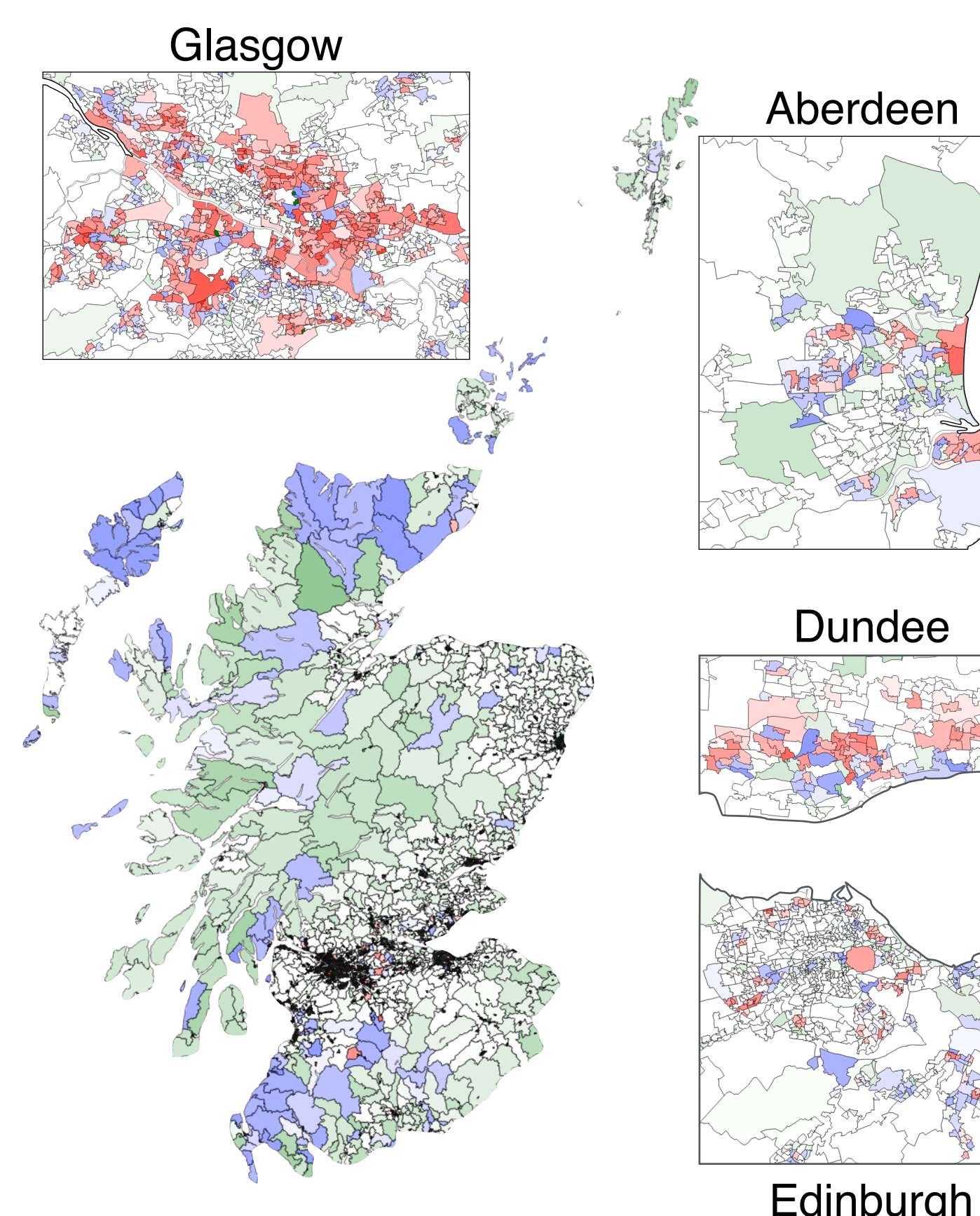
Analysing more recent ITU data for 68 countries, from 2000-2014 we find that
the breadth of the global divide is steadily growing, while the depth of the
divide, which fell from 2000 until 2011, is now rising.

Using fine-grained, postcode-level data, we have examined the distribution
of domestic broadband in Scotland, in relation to the Scottish Index of
Multiple Deprivation (SIMD). The map shows Scotland's 6505 output areas,
the insets focus on Glasgow, Aberdeen Dundee & Edinburgh. **Opacity**
represents the local depth of the divide.

Colour indicates the marginal effects of increased inclusion:

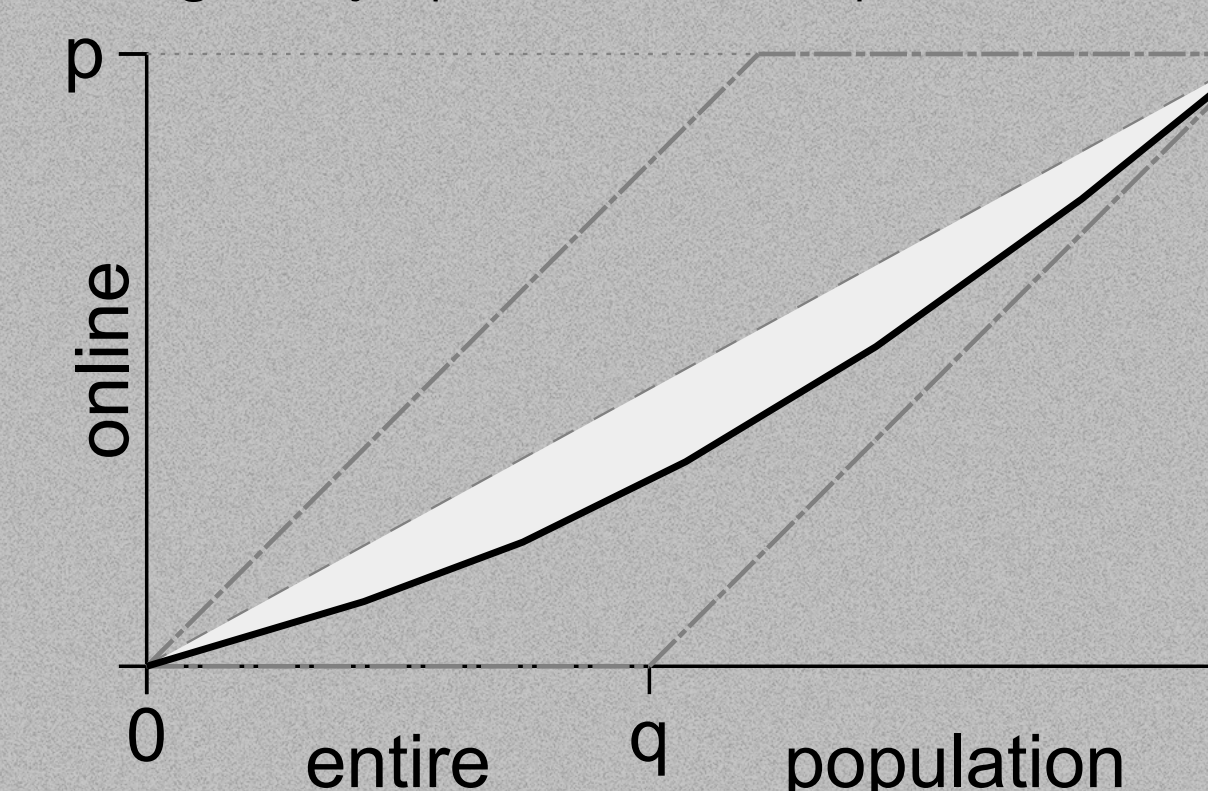
- in **red areas** it would reduce the breadth and depth of the national divide
- in **blue areas** it would reduce the breadth of the national divide, but
increase its depth
- in **green areas** it would increase both breadth and depth.

To reduce the divide, interventions must focus on the red and blue areas.



The Gini Index, or Concentration Index, C , is based on a plot of
cumulative income v. population ordered by income.

It is twice the gap between the line of perfect equality and the
Lorenz curve, as a proportion of the area, p , of the rectangle. Our
depth index measures the same area, relative to the area, pq , of the
parallelogram. Wagstaff 2005 suggests a renormalisation for binary
outcomes – dividing C by q – which is equivalent to our depth index.



Our breadth index, $4p$ times C , is Wagstaff's generalised
concentration index, which he introduced (in 1991) as an absolute
measure of inequality (we scale his index to give a range $[-1, 1]$ for
application to a binary variable).